



Rossmoyne Senior High School

Semester One Examination, 2019

Question/Answer booklet

MATHEMATICS SPECIALIST UNIT 1

Section Two:
Calculator-assumed

If required by your examination administrator, please
place your student identification label in this box

Student number: In figures

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In words

Circle your teacher's name:

Alvaro

Benko

Chua

Koulianos

Time allowed for this section

Reading time before commencing work: ten minutes

Working time: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total					100

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
3. You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
5. It is recommended that you do not use pencil, except in diagrams.
6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section Two: Calculator-assumed

65% (98 Marks)

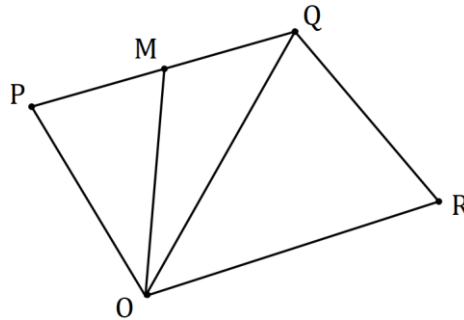
This section has **thirteen (13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9

(8 marks)

In the diagram below, M is the midpoint of PQ .



If $\overrightarrow{OP} = \mathbf{p}$, $\overrightarrow{OQ} = \mathbf{q}$ and $\overrightarrow{OR} = \mathbf{r}$, express the following in terms of $\mathbf{p}$, $\mathbf{q}$ and $\mathbf{r}$.

(a) $\overrightarrow{RP}$. (1 mark)

(b) $\overrightarrow{OM}$. (2 marks)

(c) $4\overrightarrow{RM}$. (2 marks)

(d) Determine the value of λ and μ if $4\lambda\mathbf{p} + \mathbf{q} - 2\mu\mathbf{q} = -3\mathbf{p} - 3\mu\mathbf{p} + 3\lambda\mathbf{q} + 2\mathbf{q}$. (3 marks)

Question 10

(8 marks)

- (a) Show that the vectors $\begin{pmatrix} 12 \\ -4 \end{pmatrix}$ and $\begin{pmatrix} 3 \\ 9 \end{pmatrix}$ are perpendicular. (2 marks)

- (b) Determine, to the nearest degree, the angle between the vectors $\begin{pmatrix} -1 \\ 3 \end{pmatrix}$ and $\begin{pmatrix} -2 \\ 2 \end{pmatrix}$. (2 marks)

- (c) The vectors $\begin{pmatrix} a \\ a-2 \end{pmatrix}$ and $\begin{pmatrix} a-6 \\ 4 \end{pmatrix}$ are perpendicular, where a is a constant. Determine the value(s) of a and the corresponding pair(s) of vectors. (4 marks)

Question 11**(8 marks)**

Points P , Q and R have position vectors $\begin{pmatrix} 15 \\ -6 \end{pmatrix}$, $\begin{pmatrix} -8 \\ 7 \end{pmatrix}$ and $\begin{pmatrix} 16 \\ -3 \end{pmatrix}$ respectively. Determine

(a) $\overrightarrow{PQ}$. (1 mark)

(b) $|\overrightarrow{QR}|$. (2 marks)

(c) $4\overrightarrow{PQ} + 52\mathbf{u}$, where $\mathbf{u}$ is a unit vector in the direction $\overrightarrow{QR}$. (3 marks)

(d) The position vector $\overrightarrow{OS}$ of point S , given that $\overrightarrow{SP} = \overrightarrow{RQ}$. (2 marks)

Question 12**(8 marks)**

Determine how many of the integers between 1 and 500 inclusive are

(a) divisible by 7. (1 mark)

(b) divisible by 7 or 9. (3 marks)

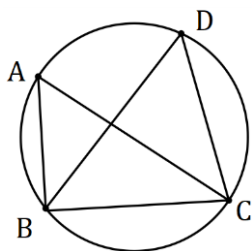
(c) divisible by 7 or 9 but not both. (1 mark)

(d) divisible by 7 or 9 but not 6. (3 marks)

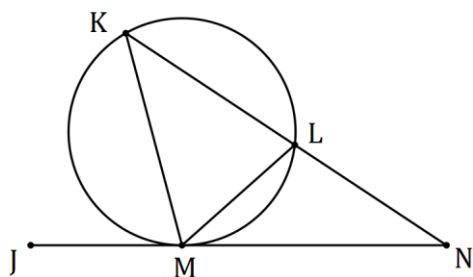
Question 13

(8 marks)

- (a) A, B, C and D lie on a circle with diameter AC (diagram not to scale). Determine, with reasons, the size of $\angle BDC$ when $\angle BCA = 40^\circ$. (4 marks)



- (b) K, L and M lie on a circle (diagram not to scale). Secant KN cuts the circle at L and JN is a tangent to the circle at M . Given that $\angle LNM = 33^\circ$ and $\angle LMN = 43^\circ$, determine the size of $\angle MKL$ and the size of $\angle KMJ$. Justify your answer. (4 marks)



Question 14**(9 marks)**

The parts of this question refer to the word BENEDICTIVE. It has 6 different consonants and 5 vowels, some of which are repeated.

- (a) Determine the number of ways that 5 different consonants chosen from the letters of the word can be arranged in a row. (1 mark)

- (b) Determine the number of ways that all the letters of the word can be arranged in a row. (2 marks)

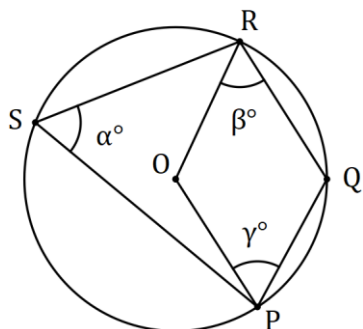
- (c) Determine the number of ways that all the letters of the word can be arranged in a row if the consonants must all be together. (3 marks)

- (d) Determine how many 3 letter permutations (e.g. TDI, EBE, etc) can be made using the letters of the word. (3 marks)

Question 15

(5 marks)

In the diagram below (not drawn to scale) P, Q, R and S lie on the circle with centre O . Determine, with reasons, the size of angles α , β and γ given that $\angle PQR = 119^\circ$ and $3\beta = 4\gamma$.



Question 16**(8 marks)**

- (a) A set of cards is numbered with all the even numbers between 100 and 998. Determine the minimum number of cards that must be selected to ensure that at least 4 cards in the selection have the same last digit. Justify your answer using the pigeonhole principle. (3 marks)
- (b) Seven different books sit on a shelf, one of which is fiction and the rest non-fiction. A student is told they can take away as many of them as they like but must not leave empty handed. Determine how many different selections can be made
- (i) of exactly 4 books. (1 mark)
- (ii) altogether. (2 marks)
- (iii) that include the fiction. (2 marks)

Question 17**(8 marks)**

A and B have position vectors $5\mathbf{i} - 10\mathbf{j}$ and $-11\mathbf{i} + 15\mathbf{j}$ respectively.

Particle P is initially at A and moves with a constant velocity of $12\mathbf{i} - 5\mathbf{j} \text{ ms}^{-1}$.

(a) Calculate

(i) the speed of P . (1 mark)

(ii) the position vector of P after 2 seconds. (1 mark)

(iii) the distance of P from B after 2 seconds. (2 marks)

(b) Determine how long after leaving A that P is 233 m from B . (4 marks)

Question 18**(7 marks)**

Three forces **a**, **b** and **c** act on a point in a plane.

The forces are $\mathbf{a} = -53\mathbf{i} + 19\mathbf{j}$ N, $\mathbf{b} = -25\mathbf{i} - 48\mathbf{j}$ N and $\mathbf{c} = 309\mathbf{i} + 231\mathbf{j}$ N.

- (a) Determine the magnitude of the resultant force and the direction, to the nearest degree, that the resultant makes with the horizontal unit vector **i**. **(3 marks)**

When $\lambda\mathbf{a} + \mu\mathbf{b} + \mathbf{c} = \mathbf{0}$, the forces are in equilibrium.

- (b) Determine the values of the scalar constants λ and μ for equilibrium to occur. **(4 marks)**

Question 19**(5 marks)**

Lay is planning a route for his sailing practice involving three successive straight legs.

The first leg from the jetty to point A is 12 km at a bearing of $026^\circ T$. The second leg from point A to point B is 8 km at a bearing of $258^\circ T$. The final leg needs to bring him back to the jetty from point B.

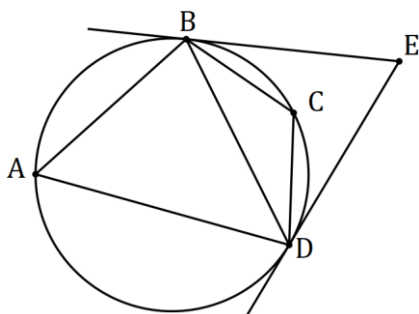
- (a) Draw a clearly labelled diagram to represent his route. (1 mark)

- (b) Determine the required distance (to 2 decimal places) and bearing (to the nearest degree) for the final leg of the route. (4 marks)

Question 20

(9 marks)

- (a) In the diagram below (not drawn to scale) A, B, C and D lie on a circle and EB and ED are tangents to the circle. If $\angle BED = 54^\circ$ and $\angle CDB = 20^\circ$, determine the size of $\angle CBD$. Justify your answer. (4 marks)



- (b) Quadrilateral $WXYZ$ is such that $YX = YZ$, $\angle XWZ = 96^\circ$ and $\angle XZY = 48^\circ$.

- (i) Sketch a diagram to show this information. (1 mark)

- (ii) Show that $WXYZ$ is cyclic and hence determine, with reasons, the size of $\angle YWZ$. (4 marks)

Question 21**(7 marks)**

Farm A lies 95 km away from farm B on a bearing of 062° . A helicopter leaves farm A at 7:30 am to fly to farm B . The helicopter can maintain a speed of 145 kmh^{-1} and there is a steady wind of 35 kmh^{-1} blowing **from** the north.

Determine the bearing that the helicopter should steer and the time of its arrival at farm B , to the nearest minute.

Supplementary page

Question number: _____

Supplementary page

Question number: _____

Supplementary page

Question number: _____

Supplementary page

Question number: _____

